Tracking for Augmented Reality on Wearable Computers

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Abstract

Wearable computers afford a degree of mobility that makes tracking for augmented reality difficult. This paper presents a novel object-centric tracking architecture for presenting augmented reality media in spatial relationships to objects, regardless of the objects' positions or motions in the world. The advance this system provides is the ability to sense and integrate new features into its tracking database, thereby extending the tracking region automatically. A lazy evaluation of the structure from motion problem uses images obtained from a single calibrated moving camera and applies recursive filtering to identify and estimate the 3D positions of new features. We evaluate the performance of two filters; a classic Extended Kalman Filter (EKF) and a filter based on a Recursive-Average of Covariances (RAC). Implementation issues and results are discussed in conclusion.

1. Motivation and Introduction

Wearable computers offer a compelling target for augmented reality (AR) interface metaphors. The promise of wearables is to endow users with essentially limitless mobility and range. Users, moving about and interacting with the real world, receive data and communication through wearables. The AR metaphor of overlaying information in spatial relationships to real objects support such interactions without the ambiguity that may arise from text or diagrams displayed in fixed screen positions. Figure 1 illustrates how spatially aligned AR overlays can concisely communicate information and tasks. Maintaining the spatial alignment between virtual annotation and real objects as users move requires dynamic tracking of the viewpoint relative to objects.



Fig. 1 Example of AR annotation supporting a maintenance task

Tracking has been at the heart of research and development in augmented reality (AR) since it's inception in the 1960's [SUTH68]. Many systems have been developed to track the six-degree of freedom (6DOF) pose of an object (or a person) relative to a fixed coordinate-frame in the environment [FOXL96, GHAZ95, KIM97, MEYE92, SOWI93, STAT96, WARD92, WELC97]. These tracking systems employ a variety of sensing technologies, each with unique strengths and weaknesses, to determine a world-centric pose measurement, as required for virtual and augmented reality applications. Tracking for AR in a fixed frame of reference, however, implies that objects in the environment are calibrated to the tracker's frame of reference and that, after calibration they remain fixed.

This assumption is valid for applications such as architectural visualization [KLIN97, FEIN95] where the walls and floors form a rigid structure whose world coordinates can be calibrated, or are already known by design, and are not likely to move. World-centric trackers can be used to calibrate movable objects [FEIN93, STAR97, WELL93, BAJU92], but this generally entails placing and calibrating tracking system elements on each object of interest and operating within range of the shared tracking infrastructure, (*e.g.*, magnetic fields or active beacons) [KIM97, WELC97]. These requirements make it difficult and expensive to accommodate moving objects with current world-centric tracking approaches.

A large class of AR applications require annotation on objects whose positions in a room or the world may vary freely without impact on the AR media linked to them. For example, AR applications in manufacturing, maintenance, and training [KLIN97, CAUD92, FEIN93] require virtual annotations that provide task guidance and specific component indications on subassemblies or portions of structure (Fig.1). These applications are particularly suited to wearable computers because of the mobility afforded to the user. A more appropriate tracking solution for these highly mobile applications is one that is object-centric, or in other words, based on viewing the object itself [NATO95, NEUM96, REKI97, SHAR97, UENO95, STAR97, KUTU96, MELL95]. Such tracking is possible with the pose estimation methods developed in the fields of computer vision and photogrammetry [HUAN94, FISC81]. However, a weakness of vision-based tracking is that pose is only computed for those views that contain known features of the scene. Given the mobility of wearable computer users, and the range of tasks they may need to perform, it is necessary to increase the robustness of pose tracking. Our tracking method can dynamically expand the range and robustness of tracked AR camera views as the system is operating.

1.1. Issues in Vision-Based Tracking

Vision-based tracking is the problem of calibrating a camera's pose relative to an object, given one or more images. Vision-based tracking methods can be roughly grouped into the three following categories, based on their requirements:

Three or more known 3D points from a single image [FISC81, GANA84, HORA89, KLIN97, KUTU96, MELL95, SHAR97, NEUM96, WARD92]

A sequence of images from a moving camera where point positions may be known or unknown [AZAR95, BROI90, SOAT94, WELC97, UENO95]

Model and template matching from a single image [LU96, NATO95]

The first class of approaches uses a calibrated camera to provide constraints to the pose formulation, so only a few known points within a single image are needed for tracking. This class of methods has been successfully employed in AR tracking systems, and it is used in our system as well.

The points needed for tracking can be object features such as corners and holes, or they can be intentionally designed and applied targets or fiducials. We selected the latter option in our work since naturally-occurring features can be difficult to recognize due to their variety and unpredictable characteristics. Also, objects do not always have features where they are needed for tracking; large regions of surfaces are often indistinguishable when viewed without context. Fiducials have the advantage that they can be designed to maximize the AR system's ability to detect and distinguish between them, they can be inexpensive, and they can be placed arbitrarily on objects. The design and detection of

fiducials are important topics, but in this work, we assume only that fiducials have some basic characteristics such as color and shape.

Our goal is to increase the range of camera-motion that provides tracked viewing while minimizing the number of fiducials that must be applied to an object. A worst-case occurs when all regions of a large object are equally likely to be viewed and therefore a dense distribution of fiducials is needed to support tracking over the entire object. Covering large objects (*e.g.*, airplanes, machinery) with fiducials is impractical and calibrating them is difficult. Our approach is an alternative analogous to "lazy-evaluation" in algorithm design; fiducials are only placed, and their positions computed, as the need for them arises. An initial set of fiducials is strategically placed and calibrated on an object or a fixture rigidly connected to an object. As regions of the object require additional fiducials to support tracking, users simply add new fiducials to those regions of interest and allow the system to automatically calibrate them. Once calibrated, the new fiducials are added to the database of known fiducials that are used for tracking. In addition to extending the range of tracked poses, the additional fiducials stabilize the pose calculation since more fiducials are likely to be visible in images.

This approach is most practical when a limited region of the object needs to be viewed and tracked for a given task, but that region and task is just one of many that may occur. Assembly, training, and maintenance tasks often have this quality. Information for a given task is local, but the specific task and locality is only one of many that may be performed by different people at different times. Figure 1 illustrates AR annotation for a maintenance task that requires tracking in only a limited region around an access panel in a larger structure. The remainder of this paper presents our vision-based AR tracking architecture. Details are given on the recursive filters that calibrate the 3D positions of new fiducials. We compare the results from two filters and two operational examples.

2. System Architecture

Figure 2 depicts our architecture. A single camera provides real time video input, and a user observes the camera image and AR media overlay on a display that may be desktop, handheld, or head-mounted. Sections 2.1 - 2.3 describe the components of this architecture that set the context for section 3 where the unique new point evaluation is described.



Fig. 2 - AR system architecture for extendible visionbased tracking. New fiducial management functions are shown against a gray background

2.1. Segmentation and Feature Detection

The important aspect of this step is that fiducials must be robustly detected and located. They are defined by a 2D screen position p and a type q that encodes characteristics such as color and shape. Our fiducial design is a colored circle or triangle [NEUM96], but other designs such as concentric circles or coded squares are equally valid [STAT96, EAGL, KLIN97, MELL95]. We use the three primary and three secondary colors along with the triangle and circle shapes to provide twelve unique fiducial types. Fiducials are detected by segmenting the image into regions of similar intensity and color and testing the regions for the color and geometric properties of fiducials. Detection strategies are often dependent on the characteristics of the fiducials [REKI97, TREM97, UENO95].

2.2. 2D Correspondence

The 2D fiducials (p,q) must be corresponded to elements in a database of known 3D fiducial positions and types(R,q). The result of a successful match is a corresponded fiducial whose 2D screen position and 3D coordinate on the object are now known (R,p,q). Fiducials observed in the image, but not corresponded to the world database, are passed on as uncorresponded fiducials and potential new points to estimate.

Computing correspondences is hard in the general case [MELL95, UENO95], and trivial if the fiducial types are unique for each element in the database. For this work, we consider only unique feature types that are trivial to correspond since our focus is on the extendible tracking portion of the architecture, however, we recognize that correspondence is a necessary function for the architecture to scale to truly useful levels.

Other researchers have proposed solutions of varying applicability to our case, and we intend to leverage from their work in the future [SHAR97, MELL95].

2.3. Camera Pose

Three or more corresponded fiducials allows the camera pose to be determined [FISC81]. The approach we use has known instabilities in certain poses, and in general provides multiple solutions (two or four) from a fourth-degree polynomial. Methods have been proposed to select the most likely solution [SHAR97]. We weight several tests to rank the possible pose solutions in terms of their apparent correctness.

The distance between the current and last frame's viewpoint is inversely proportional to a solution's weight.

The fiducials' relative pixel-areas are tested for agreement with the expected relationships based on each pose solution.

When more than three known fiducials are available, their projections under the candidate poses are compared to their measured positions.

When more than three known fiducials are available multiple pose calculations are performed for different sets of three fiducials, and the closest pairs from each calculation are highly ranked.

The result of this function is an array of poses K, ranked by the above tests, which are passed on to the new point functions (shown over gray in Fig. 2).

3. New Point Evaluation

This section details the unique aspects of this architecture that provide the interactive extension of the tracked viewing range. Given the camera pose and image coordinates of

the uncorresponded features, these features' position estimates are updated in one or two possible ways, as detailed in the next section.

3.1. Algorithms

3.1.1. Initial Estimates

For uncorresponded fiducials (p, q), the intersection¹ of two lines connecting the camera positions and the fiducial locations in the image create the initial estimate of the 3D position of the fiducial. The intersection threshold is scaled to the expected size of the fiducials. For example, if the radius of the fiducials is 0.5 inch, as in our case, the threshold is 1.0 inch. Our selection is based on the minimum distance that two distinct fiducials can be placed without overlap. Lines with a closest point of approach less than 1.0 inch are considered to be intersecting.

3.1.2. Extended Kalman Filter (EKF)

The Extended Kalman Filter (EKF) has been used in many applications, and details of the method can be found in references such as [MEND95, WELC97, BROI90].

Inputs to the EKF are the current camera pose and the image coordinates of the fiducial.

 c_k : camera pose at kth time step

 z_k : image coordinates of the fiducial at kth time step

The state of the EKF is the current estimate of the fiducial's 3D position. The real 3D position of the fiducial is constant over time, so no dynamics are involved in the KEF

¹ Since two lines in 3D space may not actually intersect, the point midway between the points of closest approach is used as the intersection.

equations. Parameters of the EKF, including the current state and its covariance matrix, are explained below.

 p_c : intrinsic camera parameters including focal length

 x_{k-1} : real value of 3D fiducial position. $x_k = x_{k-1} = x_{k-2} = \dots = x_1$

 \hat{x}_{k-1} (state): filter's estimate of the state value at (k-1)th time step (Initial state is the intersection of the first two lines)

Given $Z_{k-1} = (z_1 \quad z_2 \quad \dots \quad z_{k-1})$, $C_{k-1} = (c_1 \quad c_2 \quad \dots \quad c_{k-1})$, and p_c

$$\hat{x}_{k-1} = E(x_{k-1} \mid Z_{k-1}, C_{k-1}, p_c)$$
(3.1)

 \hat{x}_k^- (state prediction): predicted state estimate at kth time step given measurement up to $(k-1)^{th}$ time step

Given $Z_{k-1} = (z_1 \ z_2 \ \dots \ z_{k-1})$, $C_{k-1} = (c_1 \ c_2 \ \dots \ c_{k-1})$, and p_c

$$\hat{x}_{k}^{-} = E(x_{k} \mid Z_{k-1}, C_{k-1}, p_{c})$$
(3.2)

 z_k (measurement): image coordinate of the fiducial at kth time step

 \hat{z}_k (measurement estimate): estimated measurement at kth time step (See eq. 3.6)

$$\widetilde{z}_k$$
 (residual): $\widetilde{z}_k = z_k - \hat{z}_k$ (3.3)

Q (process noise): set to be a very small value for numerical stability. For example, let U_3 be 3x3 identity matrix, then $Q = 10^{-5} \ \mathcal{U}_3$

R (measurement noise): 2x2 covariance matrix

Let U_2 be 2x2 identity matrix, then $R = 2 \mathcal{P}U_2$, assuming that the measurement error variance is 2, and there is no correlation between x and y coordinates in the image space.

 P_{k-1} (state uncertainty): 3x3 uncertainty covariance matrix at $(k-1)^{th}$ time step

$$P_{k-1} = E[(x_{k-1} - \hat{x}_{k-1})(x_{k-1} - \hat{x}_{k-1})^T]$$
(3.4)

 P_k^- (state uncertainty prediction): predicted state uncertainty at kth time step given measurement up to (k-1)th time step

$$P_{k}^{-} = E[(x_{k} - \hat{x}_{k}^{-})(x_{k} - \hat{x}_{k}^{-})^{T}]$$
(3.5)

 \vec{h} (measurement function): function returning the projection(measurement estimate) of the current position estimate given the current camera pose and camera parameters

$$\hat{z}_{k} = h(\hat{x}_{k}, c_{k}, p_{c})$$
 (3.6)

H_k (Jacobian): Jacobian matrix of \vec{h}

K_k (Kalman Gain): 3x2 matrix. See equation (3.9)

The EKF process is composed of two groups of equations: *predictor*(time update) and *corrector*(measurement update). The *predictor* updates the previous $((k-1)^{th})$ state and its uncertainty to the predicted values at the current (k^{th}) time step. Since the 3D fiducial position does not change with time, the predicted position at the current time step is the same as the position of the previous time step.

$$\begin{split} \hat{x}_{k}^{-} &= \hat{x}_{k-1} \\ P_{k}^{-} &= P_{k-1} + Q \\ \hat{z}_{k} &= \vec{h}(\hat{x}_{k}^{-}, c_{k}, p_{c}) \end{split}$$

- (3.7) (3.8)
- (3.6)

Corrector equations correct the predicted state value \hat{x}_{k}^{-} based on the residual of actual measurement z_{k} and measurement estimate \hat{z}_{k} . The Jacobian matrix linearizes the non-linear measurement function.

$$K_{k} = P_{k}^{-} H_{k}^{T} (H_{k} P_{k}^{-} H_{k}^{T} + R)^{-1}$$
(3.9)

$$\widetilde{z}_{k} = z_{k} - \hat{z}_{k}$$

$$\widetilde{z}_{k} = \widetilde{z}_{k} - \hat{z}_{k}$$

$$(3.3)$$

$$\widetilde{z}_{k} = \widetilde{z}_{k} - \hat{z}_{k}$$

$$(3.4)$$

$$\hat{x}_{k} = \hat{x}_{k}^{-} + K_{k} ? \tilde{z}_{k}$$
(3.10)

$$P_{k} = (I - K_{k}H_{k})P_{k}^{-}$$
(3.11)

3.1.3. Recursive Average of Covariances (RAC) Filter

The RAC filter models each measurement as a 3D line through the current camera position and the fiducial location in the image. The 3D position estimate (X) of the fiducial is updated based on the measurement line (l). The uncertainty covariance matrix of the estimate is used in computing the update direction vector and the update magnitude of the estimate, and then recursively averaged with the uncertainty covariance matrix of the line.

To obtain the update direction of the position estimate, a vector \vec{v} from the current estimate (X) to a point on the line (l) that is closest to X is computed first. The update direction vector \vec{q} is a version of the vector \vec{v} scaled by the uncertainty of X, to move the estimate in the direction of larger uncertainty. Figure 3 shows the 2D analogy of

update direction computation. \vec{v} is scaled in directions of $\vec{1}_1$ and $\vec{2}_2$ by 1_1 and 2_2 respectively to produce \vec{q} .



Fig. 3 2D analogy of new algorithm of update direction in RAC

The update direction vector \vec{q} is computed by following the processes described below. First we find parameters (a,b,c) satisfying $a?_1^{-}+b?_2^{-}+c?_3^{-}=\vec{v}$ to represent the vector from the current estimate to the closest point on the new line in the uncertainty eigenvector coordinate system.

$$\begin{bmatrix} - & - & - \\ 1 & 2 & - \\ 2 & 3 \end{bmatrix} \begin{bmatrix} a \\ b \\ b \end{bmatrix} = \vec{v}$$
(3.12)

$$\begin{array}{l} a \\ b \\ c \end{array} = \begin{bmatrix} -1 & -2 & -3 \\ -1 & 2 & -3 \end{bmatrix}^{-1} \mathcal{F}$$

$$(3.13)$$

Then we compute (a', b', c') by scaling (a,b,c) by $\begin{pmatrix} 1 & 2 & 3 \end{pmatrix}$

$$\begin{bmatrix} a' & b' & c' \end{bmatrix} = \begin{bmatrix} 1 & 2a & 2b & 3c \end{bmatrix}$$
(3.14)

Finally, the update direction \vec{q} is obtained using the scaled components (a', b', c').

$$\vec{q} = a' \vec{?}_1 + b' \vec{?}_2 + c' \vec{?}_3 \tag{3.15}$$

The update magnitude *m* of the position estimate is

$$m = \min(d_{u}, d_{l}) \tag{3.16}$$

where d_u is the uncertainty of the current estimate in the direction of \vec{q} and d_l is the scaled distance from *X* to *l* in the direction of \vec{q} , i.e., $|\vec{q}|$.

The uncertainty of the position estimate is represented by a 3x3 covariance matrix. Each line has a constant uncertainty L_k , which is narrow and long along the direction of the line. Uncertainty is updated by recursively averaging the covariance matrices, similar to the process used in the Kalman Filter. In the Kalman Filter, the uncertainty covariance matrix is updated by performing weighted-averaging with 2D-measurement error covariance as below.

$$K_{k} = P_{k}^{-}H_{k}^{T}(H_{k}P_{k}^{-}H_{k}^{T} + R_{k})^{-1}$$
(3.9)

$$P_{k} = (I - K_{k}H_{k})P_{k}^{-}$$
(3.11)

In the RAC filter, the measurement is modeled as a line that is already in the same 3D space the estimate is in. Therefore we can eliminate the Jacobian matrix and its linearization approximation. This is an advantage of the RAC filter over the EKF, simplifying and reducing the computational overhead. Let P_k^- be the uncertainty

covariance matrix of the current estimate and L_k be that of the new line, then computation of the updated uncertainty covariance matrix P_k is simplified as below.

$$K_{k} = P_{k}^{-} (P_{k}^{-} + L_{k})^{-1}$$
(3.19)

$$P_k = (I - K_k)P_k^{-}$$
(3.20)

$$= (I - P_{k}^{-}(P_{k}^{-} + L_{k})^{-1})P_{k}^{-}$$

= $((P_{k}^{-} + L_{k})(P_{k}^{-} + L_{k})^{-1} - P_{k}^{-}(P_{k}^{-} + L_{k})^{-1})P_{k}^{-}$
= $(L_{k}(P_{k}^{-} + L_{k})^{-1})P_{k}^{-}$ (3.21)

The initial value of P_k is obtained in the same way by replacing P_k^- with L_k , resulting from the two initial line uncertainties.

3.2. Experiment and Result

Both filters appear stable in practice. The EKF is known to have good characteristics under certain conditions [BROI90], however the RAC gives comparable results, and it is simpler, operating completely in 3D world space with 3D lines as measurements. The RAC approach eliminates the linearization processes required in the EKF with Jacobian matrices.

We tested the EKF and RAC filters to find the positions of two new fiducials (refered to as red and magenta fiducials). We started with three known fiducials and two cases were tested. In the *panning* case, new fiducials were placed to the side of the known fiducials, assuming a translated region of interest. In the *zooming* case, new fiducials were placed in the center so that the user could zoom in to a region of interest.

Synthetic data sets were created, based on real camera poses captured by real camera movements. White noise of maximum 0.5 and 2.0 pixel-error were added to the measurements of the image coordinates of the fiducials. See figures 4 and 5 for the results of experiments with synthetic data sets.



Zoom Case: 0.5 Pixel White Noise

Zoom Case: 2.0 Pixel White Noise

Fig. 4 Synthetic Data: Camera movement - Zooming





Pan Case: 2.0 Pixel White Noise

Fig. 5 Synthetic Data: Camera Movement - Panning

Experiments with real data were performed in both the zoom and pan cases (figure 7).

The estimates of the filters were compared with analytic solutions, which have the minimum sum of Euclidean distances to the input lines. Figure 6 shows a 2D analogy of the analytic solution computation.



Fig. 6 2D Analogy of Analytic Solution:

The analytic solution is a point that has minimum sum of distances to the lines. In this case, the analytic solution is a point X that minimizes $d_1 + d_2 + d_3 + d_4$.



Fig. 7 Real Data: Zooming and Panning cases

A virtual camera view shows the results of the real data experiments graphically (figure 8). The lines are traces of the camera, i.e., the input lines used for RAC filter. The large spheres indicate positions of known fiducials, which were used for computing camera poses. The dark and bright small spheres represent the estimated positions produced by the RAC and EKF filters, while the black cube represents the analytic solution positions.



Pan Case: Magenta fiducial

Zoom Case: Red fiducial

The EKF result (bright sphere) appears in and the RAC filter result (dark sphere) is just to their left.

The EKF result (bright sphere), RAC filter front of the analytic solution (black cube), result (dark sphere), and the analytic solution (black cube) overlap and are not separately discernible.

Fig. 8 Virtual camera views of the results of real data experiments.

The results show that the estimates of the filters converge fast and remain stable after convergence with both real and synthetic data.

Our hardware configuration included a desktop workstation, however this system is similar in computing power to currently available portable laptops or wearables.

SGI Indy 24-bit graphics system with MIPS4400@200MHz.

SONY DXC-151A color video camera with 640x480 resolution, 31.4 degree horizontal and 24.3 degree vertical field of view (FOV), S-video output.

Our future work entails a solution to the 2D correspondence problem. This is necessary for the system to scale to greater numbers of fiducials. We also hope to improve our ability to select the correct pose solution, and we will have to address the error propagation from multiple chained fiducial estimates.

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